Dynamic overflow leakage in Archimedes screw generators

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Abstract—The dynamic overflow leakage phenomenon has been introduced in Archimedes screw generator research, but it has not been discussed in the literature in much detail. The authors sought to examine this phenomenon in greater detail by computational fluid dynamic (CFD) studies supported with experimental observations. The CFD results indicated that surface roughness had a significant impact on frictional power losses as well as overflow leakage in Archimedes screws. The results gathered and documented in this study will aide in further performance predicting model development to optimize the design and power production of Archimedes screw generator powerplants.

Keywords—Archimedes screw generator; hydrodynamic screw; computational fluid dynamics; microhydro generation; overflow leakage; thin film flow; efficiency; surface roughness

I. INTRODUCTION

Archimedes screws have been used to pump water since antiquity and have recently been used as hydro-electric generators (Fig. 1); in this latter function it is commonly called an Archimedes screw generator (ASG). The simple, robust design of ASGs has been advantageous for hydropower plants as they are easy and cost effective to manufacture, maintain, and operate, with low environmental impacts.

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ASGs were shown to be less expensive options than other hydro-turbine technologies with similar operational ranges [1]. This is because screw plants are less complex systems with coarser inflow screening requirements [2] that can be retrofitted to old mill sites and flood control dams [3].

Maintenance and operating costs for ASGs are low [4]. ASGs require less routine maintenance than other turbine technologies [5]. Regular fluid level checks are required. Routine cleaning may be required for screws installed in nutrient-rich waterways that stimulate significant algal growth on the blades and inner cylinder of the screw [6]. Major refurbishment is usually planned on a 20-30 year cycle [3], [5].

Archimedes screws are widely viewed as an “eco-friendly” hydropower option. They usually operate as run-of-river systems which have been shown to have less negative environmental impacts than conventional hydropower [7]. As well, sediment, debris, and fish can pass through an operating ASG. Most literature suggests ASGs do not significantly harm fish [8]–[11], however, one study found significant injury and mortality rates [12]. Injury and mortality tend to be the result of bad practice in site design. Design guidelines suggest practices that reduce harm, for example, by removing pinch points and installing rubberized bumpers on screw flight leading edges when tip speeds pass 3.5 m/s [13]. Further, downstream fish migration did not seem to be effected by an ASG powerplant [10], [14]. Disorientation and increased predation were not found at the outlet of ASGs [9], [11], however, a recent paper noted increased presence of a predator species downstream of an installation during parts of a study [10].

Screw generators have a relatively wide operational range for a micro-hydropower technology. There have been successful implementations of screw generators at sites with a head of \(h = 0.1\) m and a flow rate of \(Q = 0.01\) m³/s [15]. Larger sites have been successful with heads near 5 m [16] and flow rates of nearly 15 m³/s [17]. Within these bounds, ASGs usually operate between 60 % to 80 % river-to-wire efficiency [18]–[20]; however, some installations have operated at higher efficiencies [21], [22]. ASGs tend to perform at similar...
efficiencies to other technologies in this range of plant sizes [23].

During operation, water enters the top of the screw and begins to form a volume of water between two adjacent blades, this is often referred to as a “bucket” in the literature (cf. Fig. 1). Geometrically, the continuous helical volume that forms along the length of the screw between two adjacent flights is called a “chute” – multiple buckets usually form along one chute. Fill height ratio ($f$) can be used to quantify the water level within a bucket for modelling purposes

$$f = \frac{z_{wl} - z_{min}}{z_{max} - z_{min}}$$  \hspace{1cm} (1)

where $z_{min}$ and $z_{max}$ (cf. Fig. 1, Detail A) are the lowest and highest water levels possible in a bucket without overflow.

Archimedes screw generators have been described as quasi-static systems since power is produced by converting the dominantly static pressure in a bucket into rotational energy [24]. The main power losses during production are related to dynamic phenomena, such as friction between water and moving surfaces, fluid effects at inlets and outlets, and water leakage from buckets.

Performance models are documented in the literature that have been used to aide design optimization of ASG powerplants. The modelling techniques used by Nuernbergk [25], [26], Lubitz et al. [20], [27], and Rohmer [28] are generally similar. Bucket water level is evaluated and used to compute the torque corresponding to static pressure differences across the blades. Loss models are applied afterwards to correct the performance predictions. However, many of the loss modules presented in the literature could be improved with a more robust range of experimental data to aide in development.

Lost energy contains the data necessary for more in-depth overflow leakage modelling. Generally, it is difficult to gather useful real-world data from laboratory experiments and field studies; however, those studies do not contain the data necessary for more in-depth overflow leakage modelling. Generally, it is difficult to gather useful real-world data from ASGs during operation since simultaneous measurements of upper and lower water level, flow rate, torque, and rotation speed are required. Overflow modelling, also requires measurements of bucket fill height and the thin film that develops during dynamic overflow, further increasing experimental complexity.

This study investigates the factors that contribute to overflow leakage in Archimedes screw generators. The research presented in this article was conducted to improve overflow modelling techniques. The literature contains experiments and field studies; however, those studies do not contain the data necessary for more in-depth overflow leakage modelling. Generally, it is difficult to gather useful real-world data from ASGs during operation since simultaneous measurements of upper and lower water level, flow rate, torque, and rotation speed are required. Overflow modelling, also requires measurements of bucket fill height and the thin film that develops during dynamic overflow, further increasing experimental complexity.

The authors have developed a full-scale computational fluid dynamics (CFD) model that simulates ASG operation within an upper and lower basin with a dynamically meshed screw. Data from laboratory experiments and real-world ASG powerplants were collected to evaluate the CFD model. The evaluated CFD model was then used to simulate a range of surface roughness values and scale sizes of screws to lay the experimental groundwork for further overflow leakage model development.
II. METHODOLOGY

Data was gathered across a wide range of screw scale sizes as shown in Table I. As previously mentioned, simultaneous measurements of flow rate, up-and-downstream water levels, rotation speed, and torque were required in datasets for validating ASG models.

A. Laboratory Experiments

Laboratory experiments were carried out at the University of Guelph (Ontario, Canada). Measurements were all recorded digitally, then verified and documented with analogue measurements to ensure accurate datasets. The laboratory apparatus (Fig. 3) is discussed briefly in this section. Further details may be found in the literature [32].

The apparatus consisted of three water basins (the weir basin, upper basin and lower basin), an Archimedes screw, variable frequency drive (VFD) motor/generator, and instrumentation to measure and collect data during operation. The Archimedes screw was placed between the upper and lower basin. Water was pumped at a desired rate from the lower basin (the most downstream end of the system) into the weir basin (the most upstream end of the system). Flow rate was measured with a propeller-type flow meter placed within the piping between the two basins. Water upfilled in the weir basin and then passed through two parallel Cipoletti weirs into the upper basin. The water level passing over the Cipoletti weirs was measured and known weir relationships were used to estimate and verify flow meter measurements. Water then passed from the upper basin to the lower basin via the screw. Screw rotation speed was set and maintained by the VFD.

Water level in each basin was measured with digital depth sensors set in stilling wells. Depth measurements were verified using manual measurements of water level. Rotation speed was measured with a magnetic tachometer and verified with a handheld optical unit. Finally, torque was measured with a load cell and moment arm assembly. The moment arm was mounted to the VFD, and the load cell was attached between the moment arm and a fixed point on the apparatus frame.

A dataset with more than 1500 unique data points has been gathered with this experimental setup. Details are documented in the literature; this study used data from this set [32]–[36].

B. Field Measurements

Data was also gathered from four different real-world installations for this study. They will be introduced and discussed in this section in order of their scale size (i.e. from smallest to largest outer diameter).

The installation at Fletcher’s Horse World in Waterford, Ontario, Canada (Fig. 4a) is rated to produce 7.2 kW and operates as a single, fixed-speed screw in a covered and air-sealed enclosure. Sealed enclosures prevent ice build-up in colder climates and algal growth in high-nutrient waterways. Flow rate was measured at the most upstream opening of the installation’s inlet channel. An acoustic velocimeter (FlowTracker2® Acoustic Doppler Velocimeter®, Sontek, 2016) was used to sample water velocity in a grid pattern at the

<table>
<thead>
<tr>
<th>ASG Site</th>
<th>Location</th>
<th>( D_s ) (m)</th>
<th>( L ) (m)</th>
<th>( \beta ) (°)</th>
<th>( N ) (r)</th>
<th>Rated Power (kW)</th>
<th>Rated Head (m)</th>
<th>Rated Flow (m³/s)</th>
</tr>
</thead>
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<tr>
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<td>0.15</td>
<td>0.60</td>
<td>24.9</td>
<td>3</td>
<td>0.0011</td>
<td>0.22</td>
<td>0.00107</td>
</tr>
<tr>
<td>Laboratory Screw 2</td>
<td>Guelph, Canada</td>
<td>0.31</td>
<td>1.22</td>
<td>24.5</td>
<td>3</td>
<td>0.058</td>
<td>0.49</td>
<td>0.01</td>
</tr>
<tr>
<td>Laboratory Screw 15</td>
<td>Guelph, Canada</td>
<td>0.38</td>
<td>0.617</td>
<td>24.5</td>
<td>4</td>
<td>0.034</td>
<td>0.32</td>
<td>0.014</td>
</tr>
<tr>
<td>Fletcher’s Horse World</td>
<td>Waterford, Canada</td>
<td>1.40</td>
<td>4.50</td>
<td>22</td>
<td>3</td>
<td>0.72</td>
<td>1.7</td>
<td>0.54</td>
</tr>
<tr>
<td>Buckfast Abbey</td>
<td>Buckfastleigh, UK</td>
<td>2.50</td>
<td>10.5</td>
<td>26</td>
<td>4</td>
<td>84</td>
<td>4.2</td>
<td>2.8</td>
</tr>
<tr>
<td>Ruswarp Hydro</td>
<td>Whitby, UK</td>
<td>2.90</td>
<td>5.12</td>
<td>22</td>
<td>3</td>
<td>50</td>
<td>1.8</td>
<td>4</td>
</tr>
<tr>
<td>HydroSmart Srl Hydro</td>
<td>Valpagliaro, Italy</td>
<td>3.60</td>
<td>7.40</td>
<td>22</td>
<td>4</td>
<td>121</td>
<td>3.0</td>
<td>5.5</td>
</tr>
</tbody>
</table>

Table I. Laboratory and real-world screw dimensions and operating parameters.

Figure 3. University of Guelph Archimedes screw apparatus.

Figure 4. Real-world ASG powerplants: (a) Fletcher’s Horse World, Waterford, Ontario, Canada, (b) Buckfast Abbey, Buckfastleigh, Devon, UK, (c) Ruswarp Hydro, Whitby, Yorkshire, UK, (d) HydroSmart Srl Hydro, Valpagliaro, Ferrara, Italy.
inlet; measurements were then integrated about the grid to compute the inlet flow rate.

Up- and downstream water levels were measured with surveying equipment – requiring one individual to operate a manual transit and another to handle a surveying pole. Rotation speed was verified optically using a DSLR camera and adding a reference point on the installation frame. Torque was calculated from electrical power readings, rotation speed and gearbox data.

Similar methods were employed at the other powerplants. The Buckfast Abbey installation in Buckfastleigh, Devon, UK (Fig. 4b) is a moderate-sized, fixed-speed, single-screw installation. Flow rate was again found by integrating a grid pattern of velocity measurements made with the acoustic velocimeter. Multiple flow measurements were conducted at this site to develop a relationship between water level and flow rate within the inlet channel of the powerplant. Water level up- and downstream were measured with survey equipment to verify on-site gauge accuracy. The data collected from the gauges was then deemed accurate and used in the study. Rotation speed of the fixed-speed system was verified optically, and screw torque was again approximated by measuring electrical power and estimating system losses.

The Ruswarp ASG near Whitby, Yorkshire, UK (Fig. 4c), is a single, variable-speed screw. Flow rate was measured in a similar method as outline above, for three different inlet water levels. The sluice gate was manually adjusted at the inlet to modify the water level and flow rate entering the screw. A higher-resolution grid was measured for the first flow rate, and coarser grids for the two other inlet conditions. Channel geometry variation led to high uncertainty in the coarser measurements, so only the higher-resolution data was used from this site. Up- and downstream water level was again measured by on-site depth sensors and verified with surveying techniques. Rotation speed was recorded on-site and verified optically. Electrical power readings were gathered and used to approximate screw torque similarly to the other studies.

The HydroSmart Srl powerplant at the Lock of Valpagliaro, Ferrara, Italy (Fig. 4d) uses two large, identical, parallel screws. The site is very well instrumented; measurements and data are presented and discussed in detail in the literature [22], [37]–[39]. The site operators provided measured flow rate, up- and downstream water levels, electrical power, some power losses, and rotation speed. The authors visited the site to confirm conditions.

C. Numerical Simulations

A full-scale, dynamically meshed ASG was modelled as a three-dimensional, transient, two-phase Reynolds-averaged Navier-Stokes (RANS) computational fluid dynamic (CFD) simulation. The model was initially developed at the ICube Laboratory (Strasbourg, France) using OpenFOAM 5.0 [40]. The governing equations and simulation implementation are detailed in the literature [41], [42].

New modelling, formulation, and post processing techniques were adapted through collaboration between the University of Guelph and the ICube Laboratory using OpenFOAM 4.0. Details of the basic formulation of this adapted model are available in the literature [43]. The simulation domain is shown in Fig. 5.

The CFD simulations were initialized with a volume of water in the upper and lower basins, then run for 30-seconds of simulated time. Convergence was identified as the point when the torque had reached a regularly oscillating state, termed “quasi-steady state” by the authors (Fig. 6). In this state, the volume of water entering and exiting the system has equilibrated. The oscillations in torque values are due to the filling and emptying of buckets during operation at the inlet and outlet of the screw, respectively. The authors demonstrated that the amplitude of these oscillations depend on the inclination angle of the screw; steeper screws have larger oscillations at quasi-steady state [43].

Simulations were run to match the dimensions and operating conditions of the screws shown in Table I. for the model evaluation. Afterwards, simulations were carried out for seven geometrically similar screws at a range of scales. This set of simulations was developed to allow observation of scale effects on a range of ASG phenomena. This supports development of performance models to accurately predict ASG efficiency at all useful sizes.

The authors selected Laboratory Screw 2 (cf. Table I.) as the base scale since it was the most widely tested laboratory screw. The six other scale-sized models were geometrically scaled from Screw 2 dimensions. Therefore, all CFD models had the same diameter ratio (D_in/D_out = 0.532), pitch-diameter ratio (S/D_out = 1.00), pitch-length ratio (S/L = 0.260), number of
blades (N = 3), and inclination angle (β = 24.5°).

The seven scaled outer diameters are D_o = 0.148 m, 0.316 m, 0.675 m, 1.00 m, 2.00 m, 3.50 m, and 5.00 m. Additionally during this study, simulations of the D_o = 2 m scale-sized screw were conducted at a fill level of f = 1, over a range of five different surface roughness heights z_0 = 0 mm, 0.3 mm, 1.0 mm, 2.4 mm, 11.4 mm, and 37.0 mm. These roughness values correspond to Gauckler-Manning coefficients of n = 0, 0.010, 0.012, 0.014, 0.018, and 0.022, respectively. These values were selected since they represent the range of surface roughness values that could practically be observed in real-world installations. The highest values represent a screw with substantial algal growth on the blades and inner cylinder.

III. RESULTS AND DISCUSSION

A. CFD Model Evaluation

Results of the numerical simulations were compared to the experimental data (Fig. 7). The model seemed to perform well as it predicted similar power production values compared to the experimental data. There are small differences in the results. The CFD model is a “perfect” geometrical representation of an Archimedes screw; even given a surface roughness, there are no imperfections or slight differences within the tolerable range of manufacturing that occur in a real-world screw. As such, the gap width (Gw, cf. Fig. 1, Detail C) may differ slightly between simulation and reality – causing some differences in gap leakage loss. Frictional losses and entrance losses may, in turn, exhibit similar differences. Further, flow rate was set to match between the experiments and simulations, so any uncertainty or error in the on-site flow measurements was propagated through the numerical simulations. Nonetheless, the comparison in Fig. 7 suggests that the CFD model successfully approximates the performance of Archimedes screw generators. Therefore, the authors suggest the model is a reasonably accurate approximation of the performance of ASGs, and it is appropriate for further analysis and model development.

B. Dynamically Impacted Losses

The numerical simulations provided new insight into the mechanics of ASG power losses, including those related to gap leakage, friction loss, and overflow leakage.

The authors recently demonstrated that rotation speed drives the relative velocity of fluid flowing through the gap region [24], meaning gap leakage rate is affected by rotation speed. Since this region is occupied by a gap only, no blades can convert pressure to rotation. Thus, the gap region does not contribute to energy production, but leakage loss may be minimized to decrease its impact on power production. It was theorized that at very high speeds, the blades may “outrun” the gap leakage rate, and cause negative gap leakage [24]. At an intermediate point there may be an optimal operating point with regards to gap leakage.

Fig. 8 shows friction loss as a function of surface roughness in the D_o = 2 m scale-screw, with all variables in non-dimensional form. Power production (P_s) was non-dimensionalised by the available power (P_a), yielding the mechanical efficiency (η):

\[ \eta = \frac{P_s}{P_a} = \frac{T\omega}{\rho ghQ} \]  

(3)

where the available power is the product of water density (\(\rho\)), the gravitational constant (g), overall head (h) and total flow rate (Q). For reference, mechanical shaft power is shown in its base terms of torque (T) and rotation speed (\(\omega\)). The frictional power loss was non-dimensionalised by the available power as well to keep the two variables in the same terms.

The Darcy-Wiesbach friction factor (f_D) was used to represent the surface roughness in dimensionless terms. It was computed with the Colebrook-White equation, which requires an iterative solution in terms of surface roughness (z_0), length-scale (D_h), and the Reynolds number (Re):

\[ \frac{1}{\sqrt{f_D}} = -2 \log \left( \frac{z_0}{3.7D_h} + \frac{2.51}{Re\sqrt{f_D}} \right) \]  

(4)

In Fig. 8, surface roughness had a significant impact on power production and power loss. Intuitively, as surface roughness increased, frictional power loss increased, and overall power production dropped. Fitting a trendline to the curve suggested that frictional power loss followed a similar trend to that of a 2nd order system. This seemed like an appropriate result since friction loss is a function of area – itself
the second order of a length-scale.

The changing frictional loss is expected to affect other loss modes. The literature has some discussions of a frictional leakage flow that forms by water adhering to the blades of the screw [26], [30]; but modelling of this phenomenon seems sparse. It is suggested that this frictional leakage is a dynamic form of overflow leakage – the authors have referred to it as “dynamic overflow leakage”. This loss was impacted by surface roughness and is explored in further detail below.

C. Overflow Leakage

As mentioned, overflow leakage has two forms, static and dynamic overflow leakage; Fig. 9 demonstrates both forms of overflow leakage. Though the ASG in Fig. 9 is operating at \( f = 1 \), it still experiences static overflow leakage due to a “sloshing” phenomenon within the buckets. The bucket water levels vary along the length of the screw. This is because the water in the buckets were sloshing as it translated along the screw from inlet to outlet, due to wave formation during water inrush to the screw entrance. The sloshing caused cases of

Figure 9. CFD simulation results of the \( D_o = 2 \) m scale-size screw operating at \( f = 1 \) with a surface roughness of \( n = 0.014 \). Rotation direction is indicated on the bottom right screw blade.

periodic static overflow as the water level on the downstream end of the bucket (the high side, i.e. the +x side of Fig. 9 or the left side of Fig. 10) surpassed \( z_{max} \) (i.e. \( f > 1 \) locally) and instantaneously overflowed. The water level then sloshed back causing a case where local \( f < 1 \). This can also be observed in Fig. 10.

Fig. 10 demonstrates the mean, min, and max water levels observed within one bucket during operation. The bucket water level was tracked as it translated along the length of the screw from inlet to outlet. The water level varied significantly after the bucket was formed at the inlet and before it emptied at the outlet of the screw. This suggested that static overflow can occur when the screw operates in regimes that should not induce static overflow (i.e. when \( f \leq 1 \)) if no sloshing was observed.

The sloshing phenomenon was induced at the inlet of the screw as can be seen in Fig. 11. Water rushed into the bucket from the up- to downstream side of the bucket; the dynamic rush of water caused a higher water level on the downstream end of the bucket at first. Once the bucket was fully formed (closed off from the inlet), water no longer entered from the inlet – it then rushed back towards the upstream end of the bucket. The backrush of water caused a higher water level at the downstream end of the bucket. This process carried on, and presumably dampened as the bucket translated through the screw. It then emptied at the outlet of the screw. Interestingly, as surface roughness increased, overflow leakage decreased and became negative (Fig. 12). The negative component of overflow leakage is associated directly with dynamic overflow leakage.

Figure 11. Fill height ratio of the up- and downstream side of the bucket as it traverses the length of the screw. Time is in reference to simulation time; the simulation converged at 19 seconds and this bucket was tracked between 25 and 30 seconds.

Figure 10. Visualization of water level within one bucket during transit of bucket from inlet to outlet. (\( D_o = 2 \) m scale-screw with a surface roughness of \( n = 0.014 \)) Observing bucket in the \( xy \) plane in the +z direction (cf. Fig. 8). Solid blue lines are mean free-surface level, while dashed blue lines indicate the maximum and minimum levels observed.

Figure 12. Dimensionless overflow leakage with respect to dimensionless surface roughness.
It seemed that the periodic overflowing was minimized since the rougher walls caused greater wall shear stress and higher frictional effects. In fact, as the roughness increased, cases of negative overflow occurred – water was drawn back up from a downstream bucket along a chute to the previous upstream bucket. Fig. 12 demonstrates the significant impact that surface roughness had on static and dynamic overflow leakage. It seems that rougher walls might have dampened the sloshing effect that caused periodic static overflow and increased the formation of thin films on the blades and inner cylinder associated with dynamic overflow leakage (or friction-leakage).

This phenomenon was observed in operating screw plants, including at Buckfast Abbey (Fig. 2a) and at Romney Weir, Windsor, UK (Fig. 2b). Thin films of water can be observed on the screw blades in both images. Fig. 2a also displays the varying bucket water levels that were observed in the CFD simulations. Qualitatively, it seems that a very large amount of water was drawn up the blades at the Romney Weir (Fig. 2b). The operator of the installation noticed that periodically the screw surfaces get covered by significant algal growth, which would increase blade surface roughness. The operator noted that when the blades were cleaned and the algae was removed, an 11% increase in power production was measured [6]. Similar power increases were noticed at other sites after cleaning and removing algae from the blades and inner cylinder [44], suggesting that the combined effects of friction losses and dynamic overflow leakage were very significant.

Frictional losses have been accounted for in the literature [20], [26], however, overflow is currently only modelled statically [26], [29]. The CFD simulations described in this article will be used for further development of screw performance models by adding capabilities to account for screw rotation speed and thin film development on the blades and inner cylinder.

IV. CONCLUSION

Frictional losses and overflow leakage in an Archimedes screw were shown to be significantly impacted by changes to screw surface roughness. Overflow leakage transitioned from positive (flowing into the downstream bucket of the chute) to negative values (flowing back into the upstream bucket of the chute) as roughness increased for a screw operating at an average bucket fill ratio of $f = 1$. Positive overflow is associated with static, water-level-based overflow. Conversely, negative overflow is associated with dynamic overflow leakage through friction-based thin-films. Therefore, the change from positive to negative overflow indicated that dynamic overflow leakage was more dominant than static overflow leakage when surface roughness values were $n \geq 0.012$ (corresponding to smooth steel or rougher) for this specific set of simulations. The authors suggest that most ASGs have blade roughness values corresponding to painted steel ($n = 0.014$) or higher, depending on levels of algal growth and fouling. Significant dynamic overflow leakage was observed in real-world screws, suggesting dynamic overflow leakage is a common phenomenon, and additional modelling is required to account for it in current performance prediction models. Further research will focus on using the data and analyses from this study to aide in model development so overflow leakage (including both static and dynamic modes) may be predicted more accurately. Accurate performance predictions allow designers to optimize screw plant design to make powerplants more economically efficient.

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